

Quantum Korea | 2024

June 27, 2024



# Towards industry-relevant (quantum) applications on Pasqal QPUs

A. Andrea Gentile, Head of ML Quantum Models

# PASQAL: from the lab to an integrated Product Ecosystem



**>40+**

**CLIENTS & PARTNERS**

Multiple QPUs sold via EU HPCQS framework, activities in more than 10 countries, and engagements with top cloud distributors

**→10k**

**QUBITS**

Over 1000 qubits demonstrated, concrete path to 10,000

**55+**

**PATENTS & APPLICATIONS**

800+ publications

**230+**

**EMPLOYEES**

18 nationalities

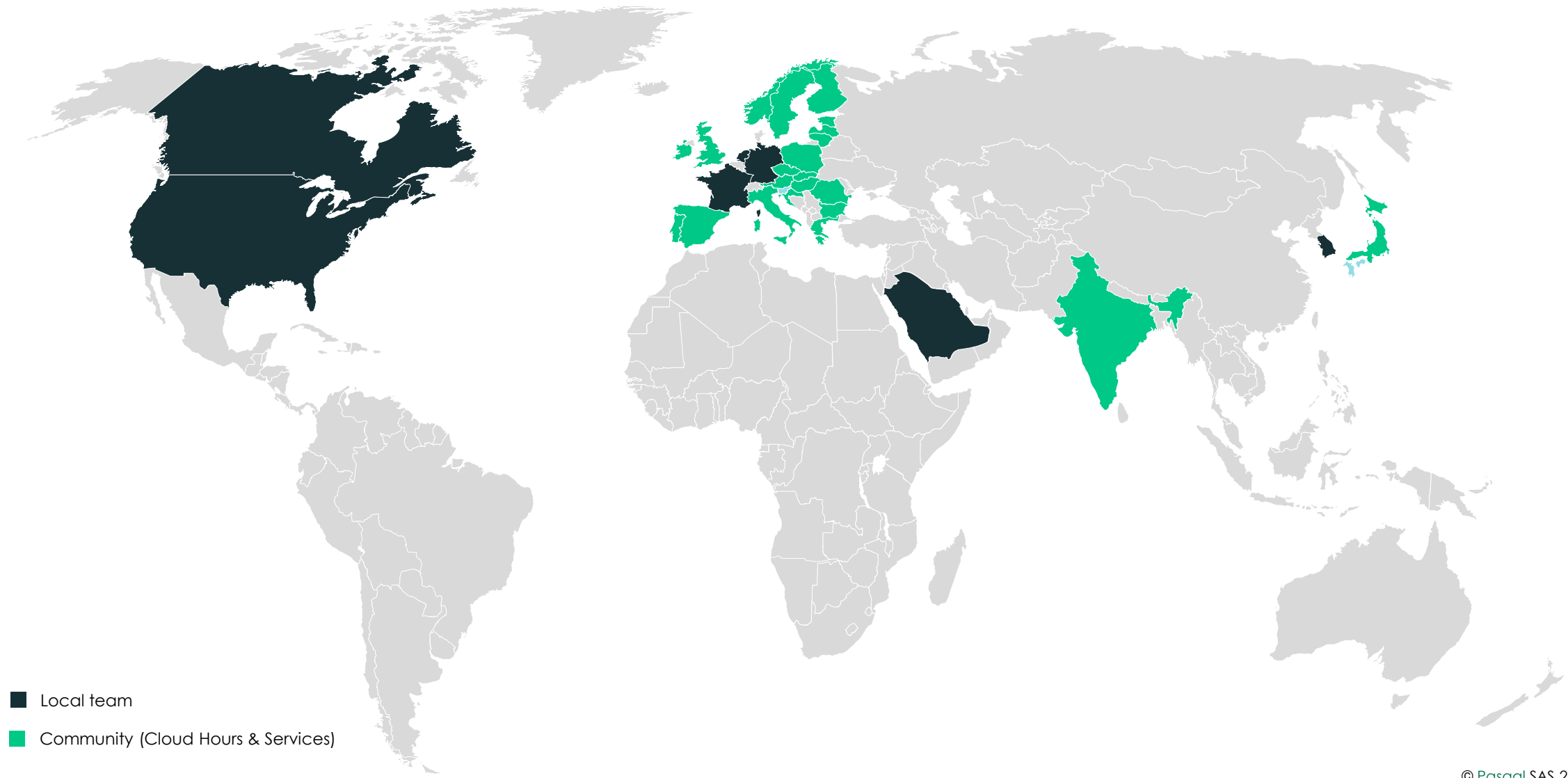
**FULL-STACK**

**QUANTUM HARDWARE & SOFTWARE TODAY**

Aiming for Practical Quantum Advantage



# PASQAL's Global Presence



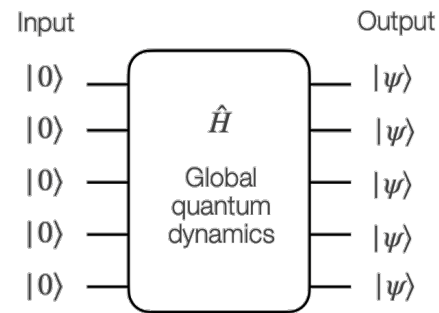
- Local team
- Community (Cloud Hours & Services)

# Neutral Atom QPUs can implement Algorithms with High Number of Equivalent Gates

## Analog Control

### Programming a Hamiltonian sequence

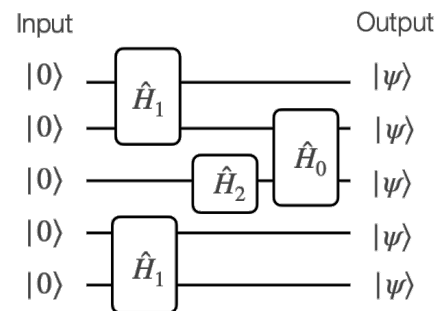
The Hamiltonian faithfully describes the dynamics of a physical quantum system or a reformulation of an operational case. Parameters can be tuned continuously.



## Digital Control

### Programming a quantum circuit with digital quantum gates

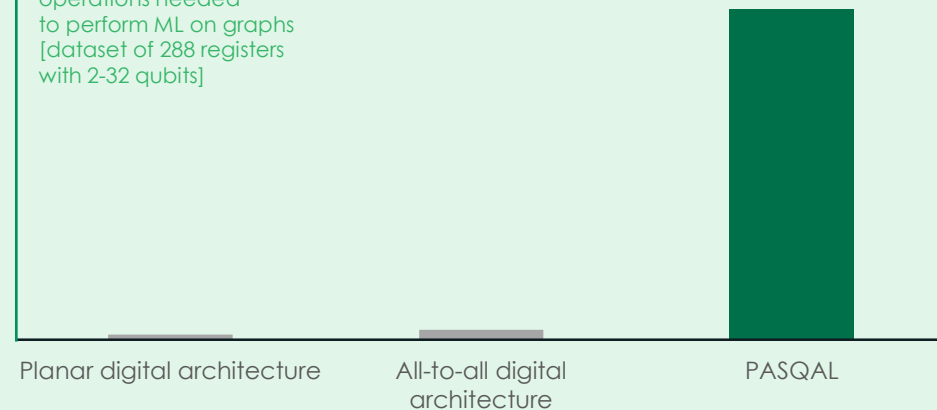
Elementary operations are discrete digital quantum gates, that can act either on individual qubits, or on several qubits at the same time.



Due to reconfigurability, PASQAL'S QPU needs 10,000x to 20,000x less operations than other QPUs to perform graph ML algorithms<sup>[1]</sup>.

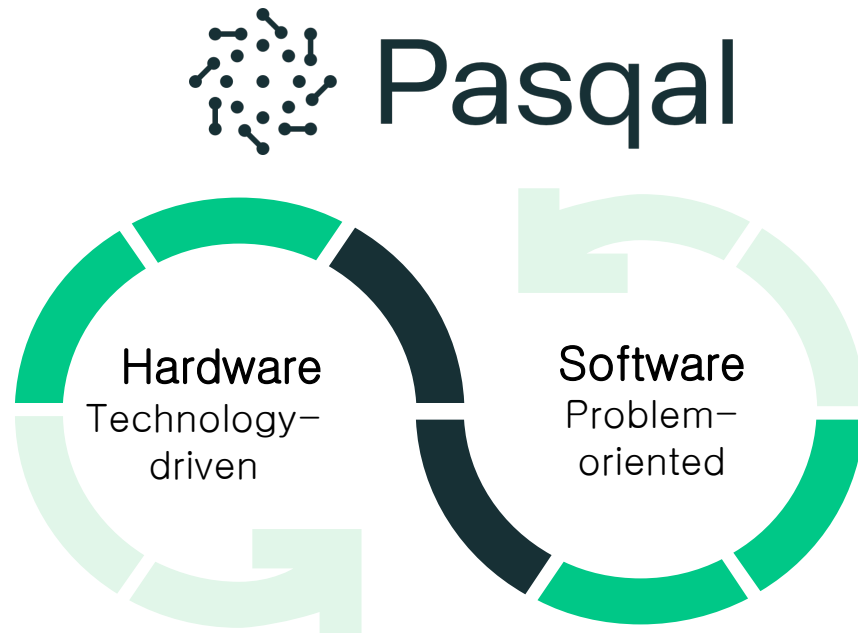
Efficiency based on the number of quantum operations needed to perform ML on graphs [dataset of 288 registers with 2-32 qubits]

Up to 20,000x more efficient than other technology



[1] Albrecht, et al., Phys. Rev. A 107, 042615 (2023)

# Combining Hardware & Software



Co-developing hardware and software

## Quantum Simulation

- Spin model dynamics (Ising/XY). In 2021, IOGS/CNRS lab implemented quantum Ising model beyond what could be simulated classically [1].
- Chemistry & Material Science Applications

## Graph Machine Learning

- HW-native Quantum Evolution Kernel (QEK) [2].
- Extensions to state-of-art graph ML models (*graph transformers, shortest path, ...*)

## Optimization

- Graph-based optimization problems (*MIS, MaxCut, ...*)
- Quantum Extremal Learning (QEL) Combinatorial optimization

## Differential Equations

- Differentiable Quantum Circuit (DQC) proposal [3].
- Many extensions including *stochastic* differential equations.

[1] Scholl, et al., Nature volume 595, pages 233–238 (2021)

[2] Henry, et al., Phys. Rev. A 104, 032416 (2021)

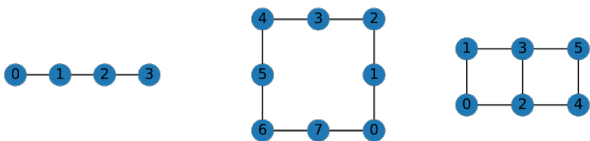
[3] Kyriienko, et al., Phys. Rev. A 103, 052416 (2021)

# Developing an open-source SW community



A library for Digital-Analog circuit design

- Automatic Differentiability via PyTorch integration.
- Parametric quantum programs with an intuitive symbolic system
- A simple interface to work with neutral-atom qubits using arbitrary registers topologies.



Design and simulate pulse sequences for neutral atoms QPUs

- Programmable atomic arrays
- Control over relevant physical parameters
- Simulation with noise and errors

and more...

- State-vector emulators interfaceable with Qadence and Pulser (PyQ, QuTip)
- Tensor-network-based emulator upcoming (Q4 2024)
- Algorithmic libraries upcoming (2025)

# Quantum Age today: industry-relevant use cases

PASQAL develops quantum solutions in collaboration with several clients and partners. Among others:



Example partners:



Example partners:



... And many others!

# Solving Differential Equations

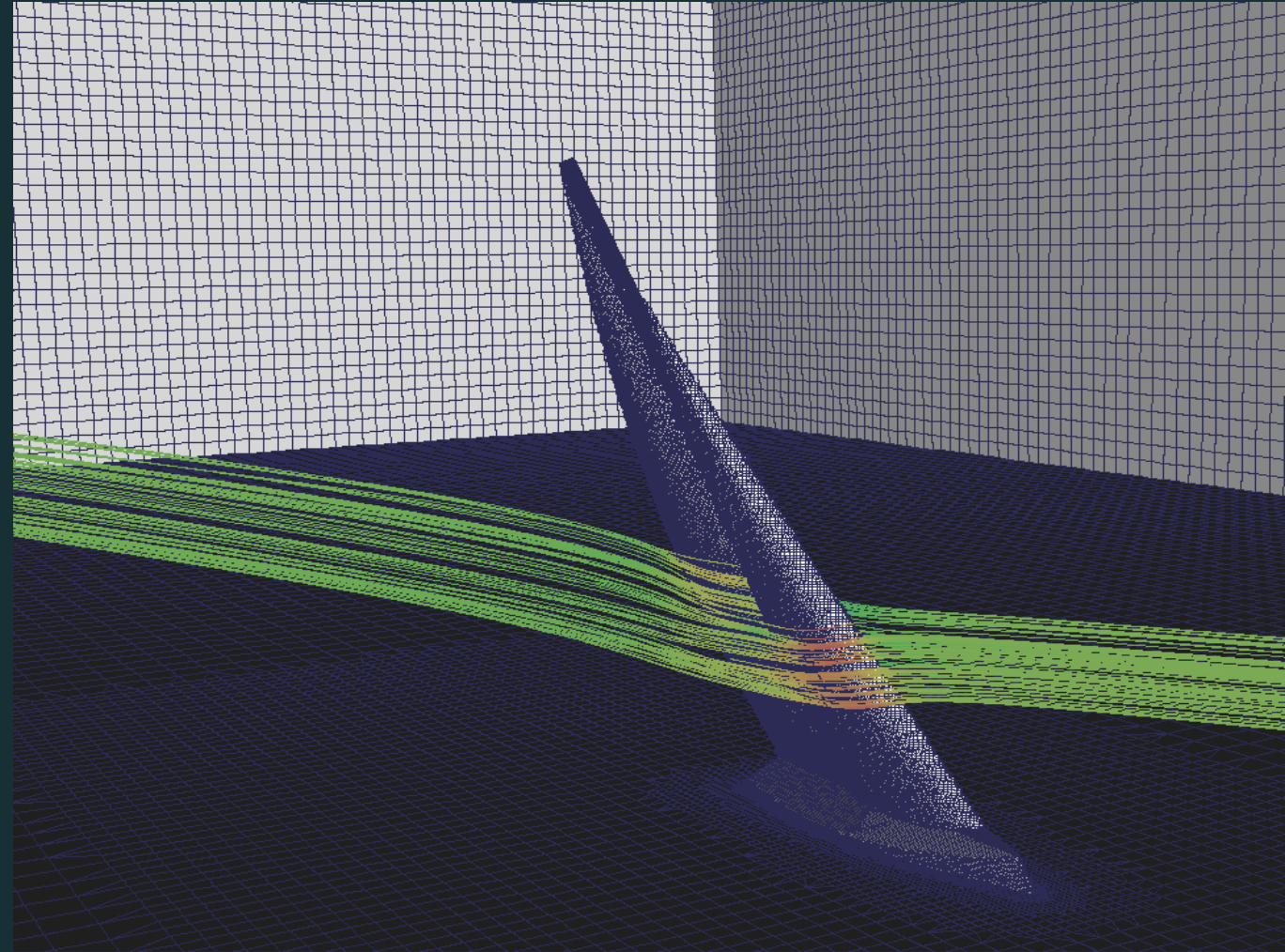
## Problem Introduction

Solve (sets of partial) differential equations modelling physical phenomena or socio-economic processes

## Goal

Surpass the limitations of state-of-art approaches and address instances which require unfeasible amount of classical computing power

In collaboration with:



# The limitations of grid-mesh based methods

When modelling exemplary physical systems

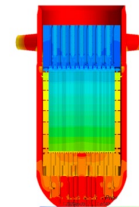
Thermal fatigue  
in T-junction,  
Eulerian approach



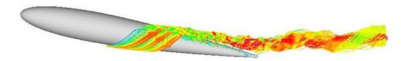
**Golf ball**  
aerodynamics at  
DNS accuracy



**Nuclear fuel  
assembly**  
at LES accuracy



**Aerospace**  
modelling  
at DNS accuracy



~mins

~hours

~weeks

intractable

Time (on  $> 10^3$  cores)

~GB

~100s GB

~10s TB

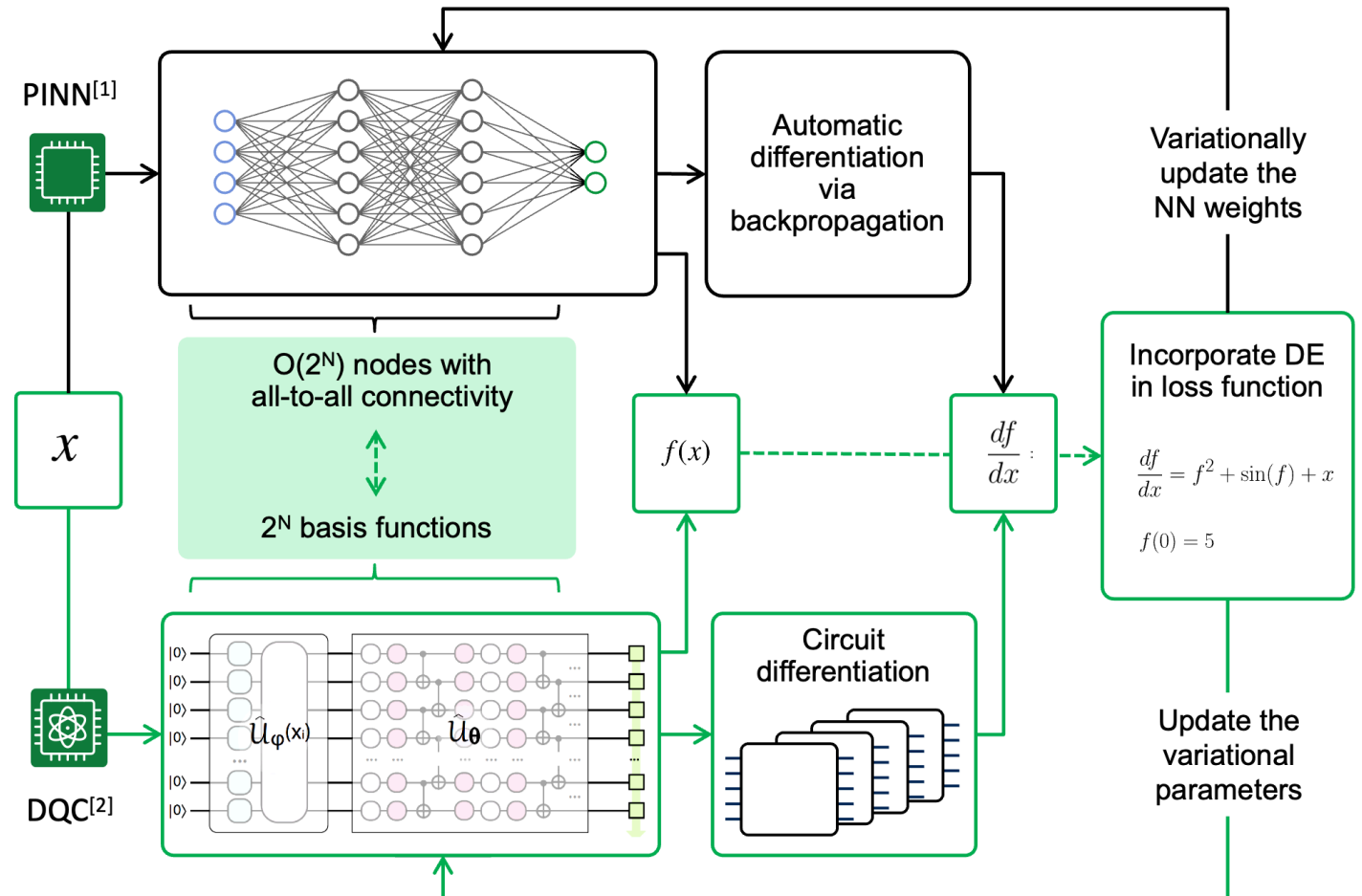
unfeasible

Memory

# (Quantum) Scientific Machine Learning

## Methodology

- Physics-Informed Neural Networks: a ML-based approach to solve differential equations.
- A neural network acts as a **function approximator**, optimized by minimizing the residual of the differential equation.
- Highly-expressive classical NNs require an **exponentially large number of nodes** with high connectivity.
- **Differentiable Quantum Circuits (DQC)** [1] give access to highly-expressive **function approximators** with much fewer qubits

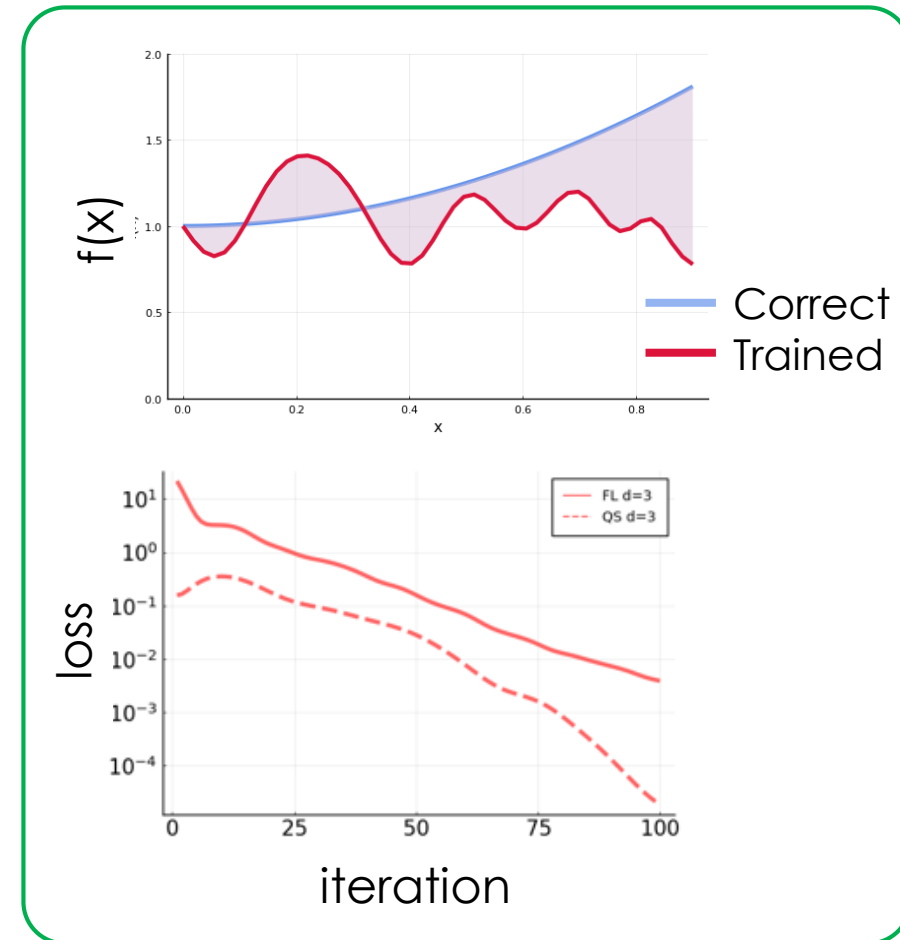


[1] Kyriienko et al., Phys. Rev. A 103, 052416 (2021)

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# Computational Fluid Dynamics (CFD)

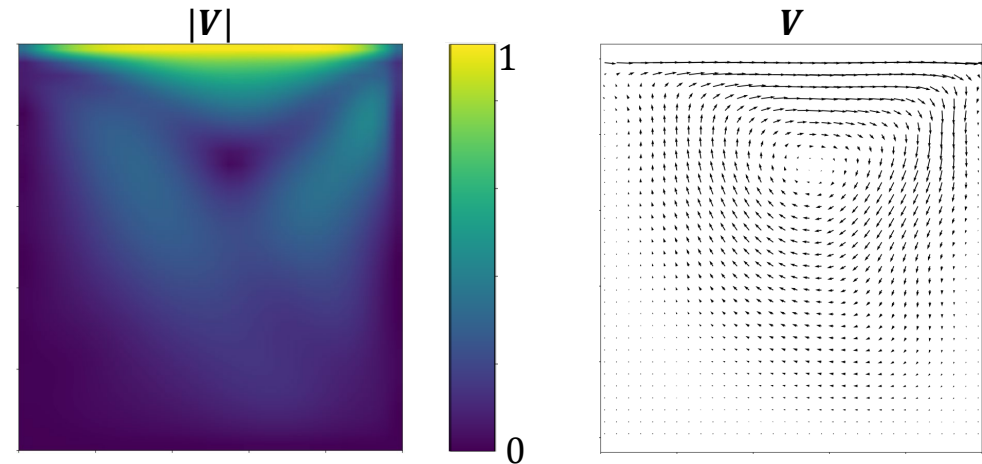
## Problem Layout

- CFD solutions can pose severe challenges for mesh-based (e.g. FEM) solvers, when the “Reynold number”  $Re$  describes turbulent regimes
- We test DQC by solving for the fluid velocity  $\mathbf{V}$  in steady-state ( $\partial \cdot / \partial t = 0$ ) **incompressible Navier-Stokes** eq.:

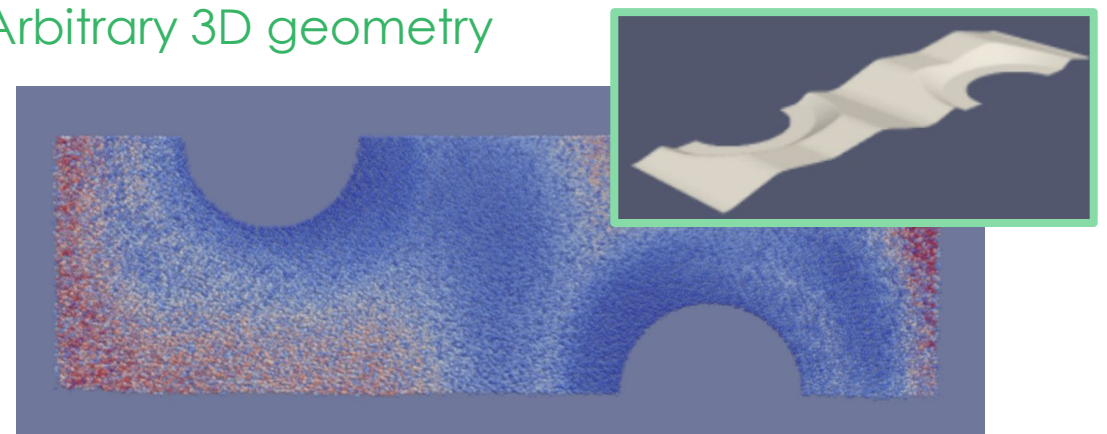
$$\frac{\partial \mathbf{V}}{\partial t} + (\mathbf{V} \cdot \nabla) \mathbf{V} = -\nabla p + \frac{1}{Re} \nabla^2 \mathbf{V}$$

- We use **DQC with  $O(10)$  qubits** to solve paradigmatic lid-driven geometries up to  $Re \sim 500$  as well as complex geometries
- We achieve good agreement with FEM benchmarks

## Lid-driven cavity



## Arbitrary 3D geometry



# Industrial Process optimization

Problem Introduction

Producing  $H_2$  from ammonia cracking

## Goal

Minimize power consumption and hazardous emissions while maximizing production

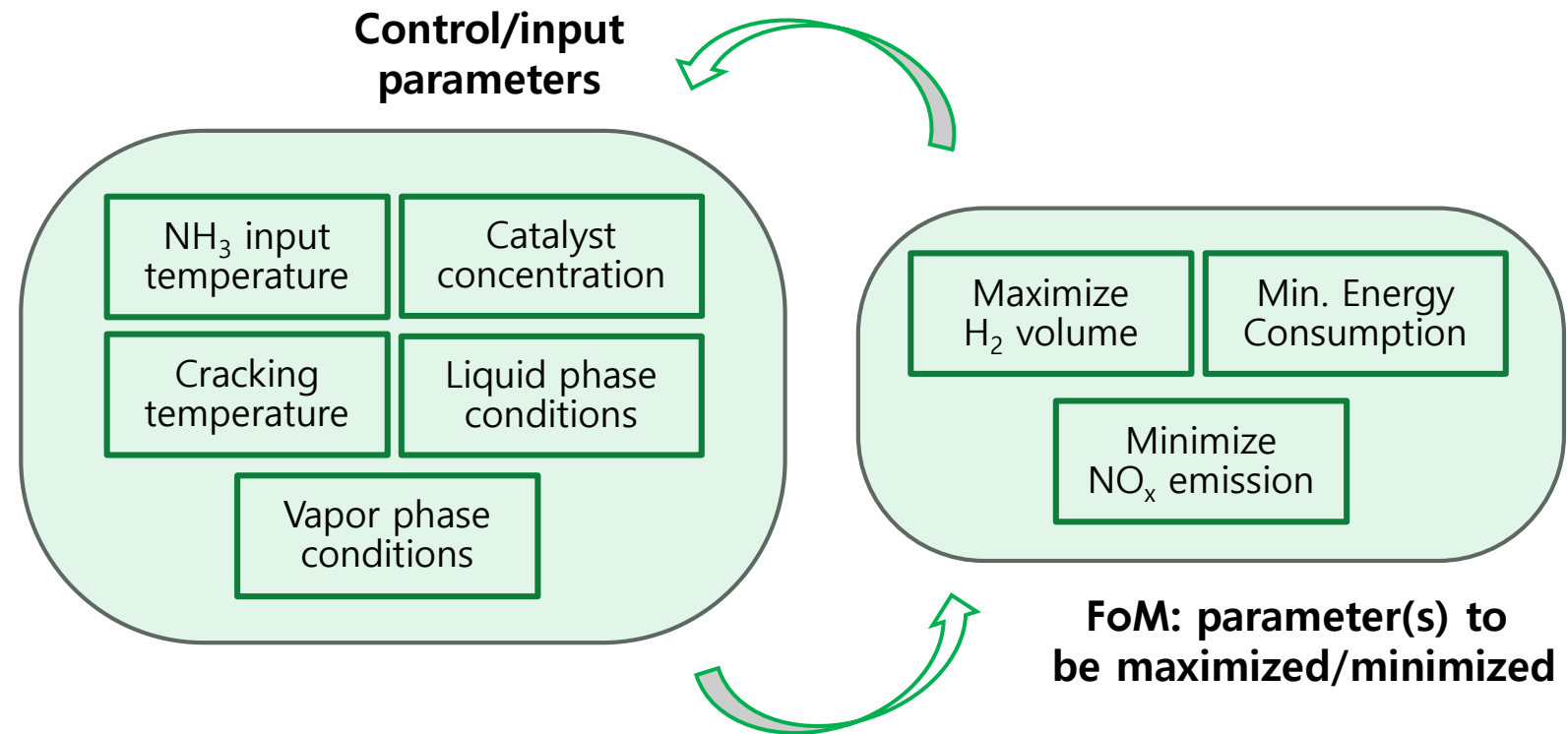
In collaboration with:



# Process optimization of a chemical plant

## Problem setting

- Some key Figures of Merit (FoM) are controlled by tuning a finite set of process parameters
- Maximising the FoMs predicted by a (here, unknown) model is an **extremization** process that can involve continuous or discrete parameters
- Pasqal's Quantum Extremal Learning (QEL) is ideally suited to target this problem



# Quantum Extremal Learning (QEL)

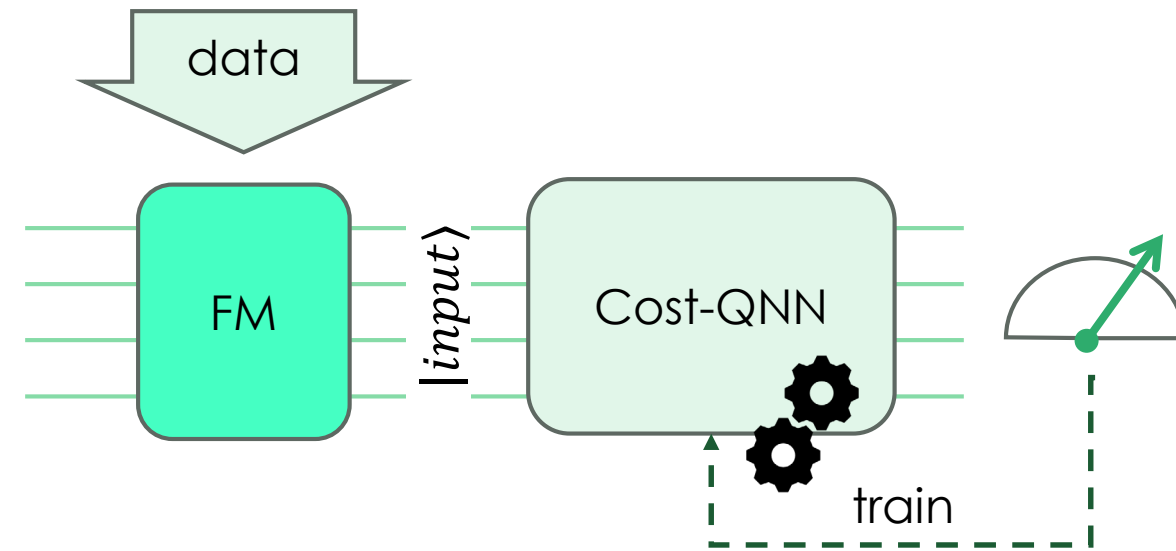
## Methodology

QEL [1] addresses the challenge of not only modelling the data but **finding the input to a hidden function** that extremizes the function output, **without having direct access to said function**, but **only to partial input-output data**

**Why?** this approach becomes use-full when we are looking for a high dimensional extremal point

QEL works in two main steps:

- **Train QNN:** a parametric **quantum circuit (cost-QNN)** is variationally trained to model data input-output relationships by reducing a **loss**



# Quantum Extremal Learning (QEL)

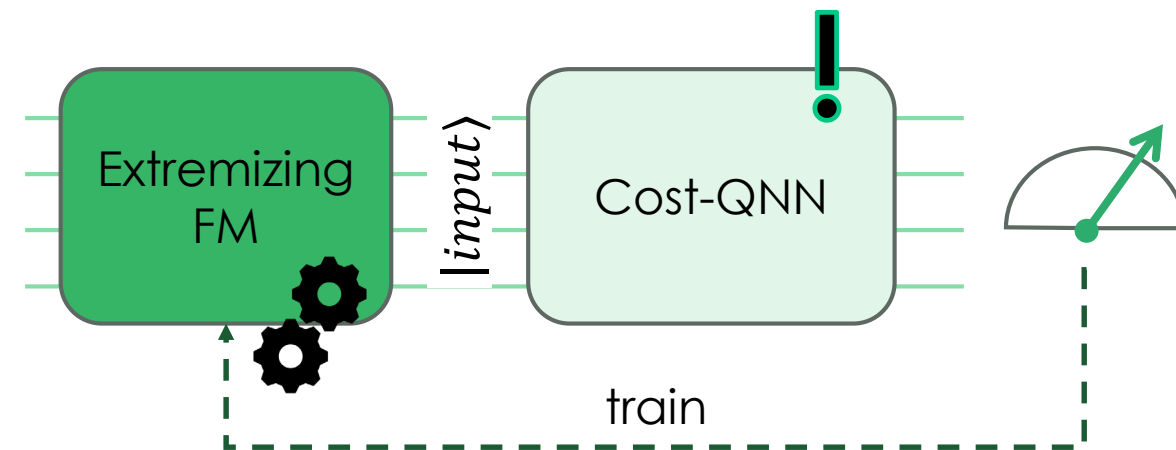
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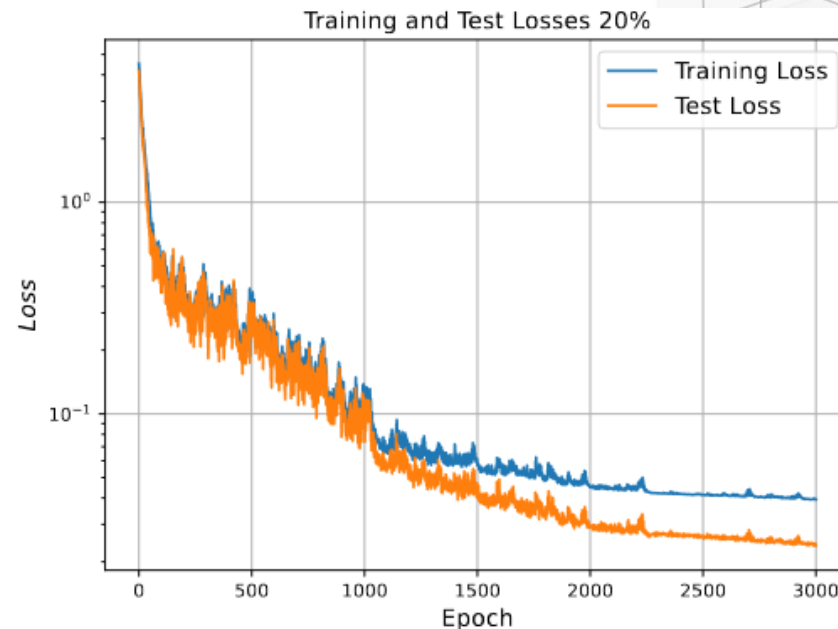
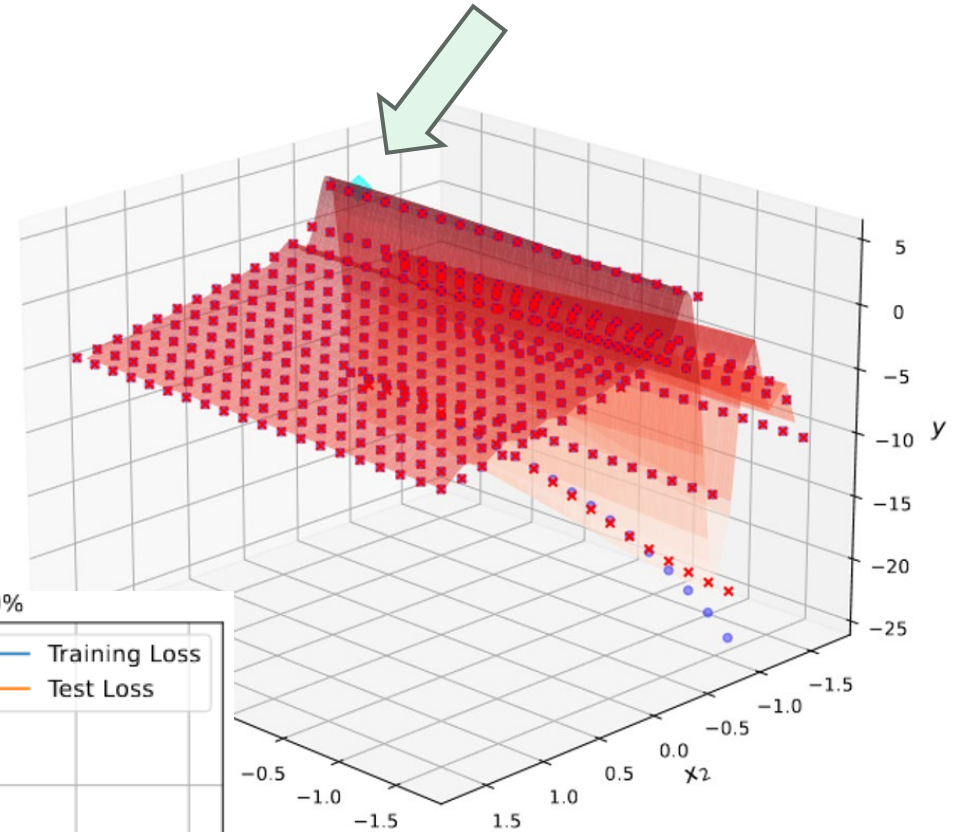
- **Find extremal point:** a trainable Extremizing Feature Map, encoding input data, is analytically differentiated to find the extremizing coordinate



# Process optimization of a chemical plant

QEL in action

- Optimization instance with 2 independent control parameters
- Analysis with a 6-qubit, depth-10 cost-QNN
- Training adopted: 320 pts
- We checked the generalization capabilities of the model by performing the Testing on: 80 pts





# Mission planning for Satellites

Quantum computing  
for earth observation

In collaboration with:



# Combinatorial optimization for satellites

## Problem Introduction

A constellation of satellites with defined trajectories

A set of missions to execute:  
pictures of specific cities to be taken

A set of constraints:

- daytime pictures without cloud coverage
- high-priority missions first
- allow change of plans during the day

## Goal

Maximize the number of missions accomplished in a day while respecting the set of constraints

■ Mission unaccomplished

■ Mission unaccessible

■ Mission accomplished

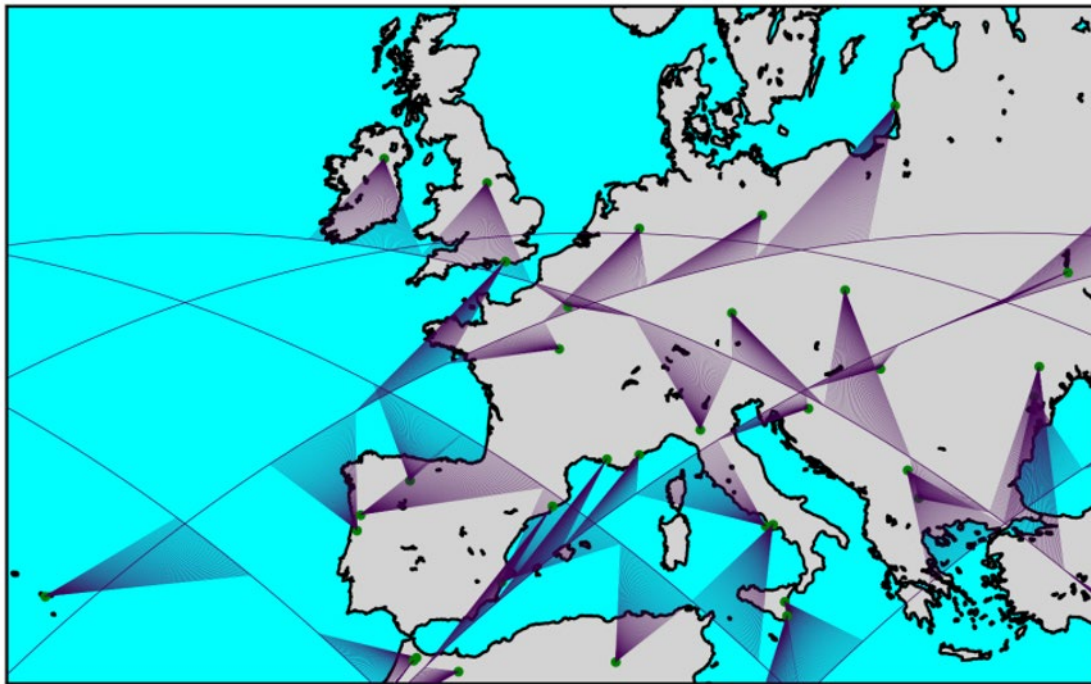


# Extending the problem to multiple satellites requires better performing solutions

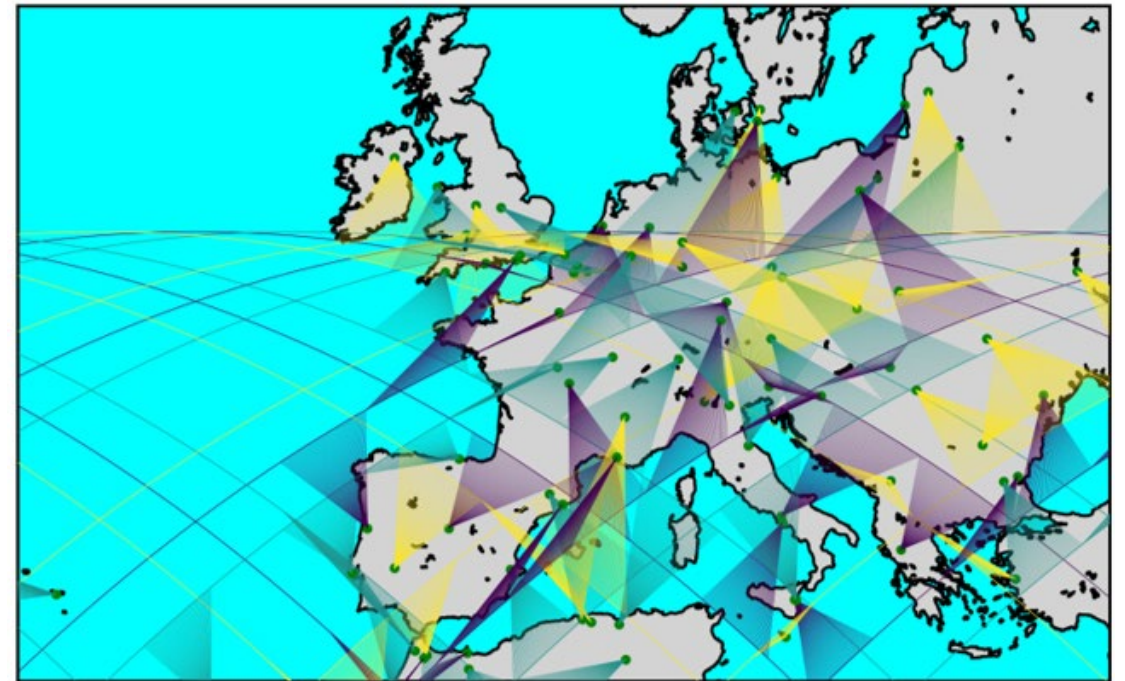
Problem Introduction



1 satellite



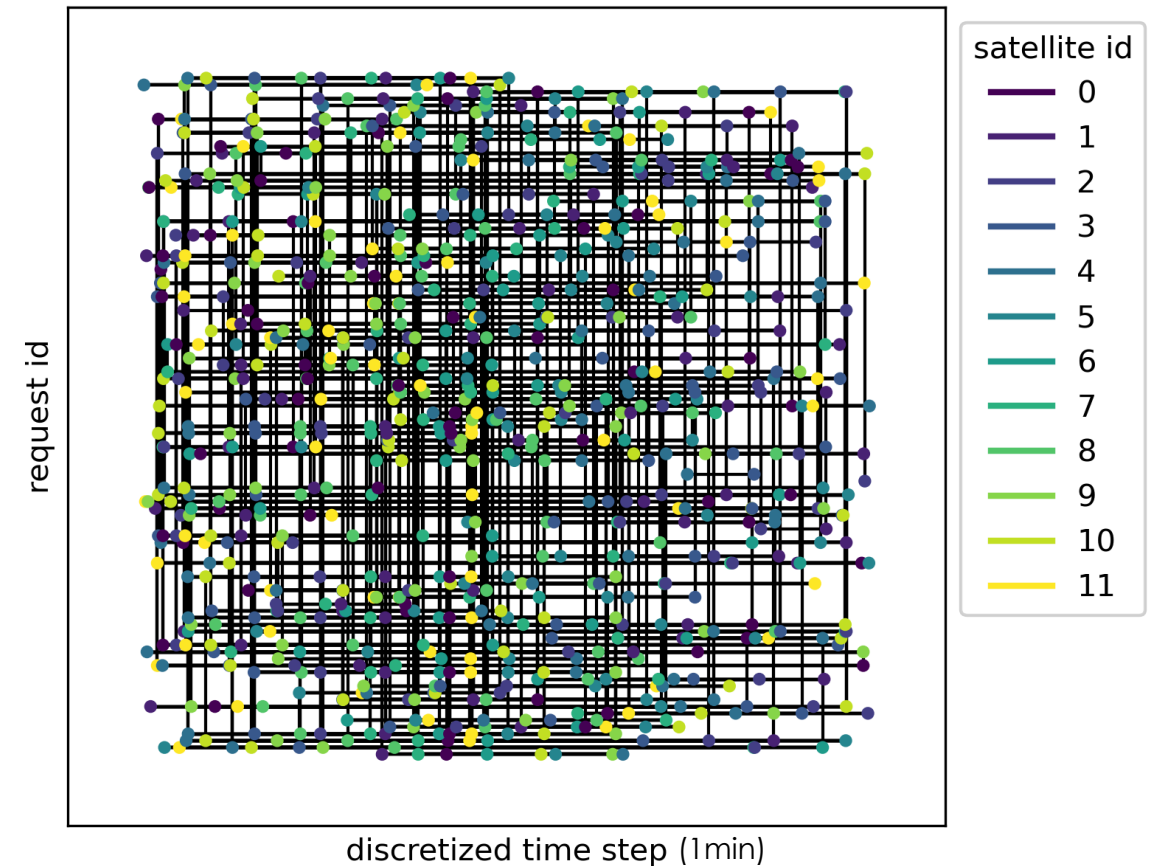
3 satellites



# Encoding the problem in a Graph Structure

- Nodes are equivalent to mission slots
- Colors represent unique satellites of the constellation
- Edges are equivalent to incompatibilities of constraints
  1. Each request performed only once
  2. No overlapping time slots per satellite
- To retrieve the solution we apply a **Maximum Independent Set** graph methodology [1,2]

Visiting capitals with 12 shifted ISS

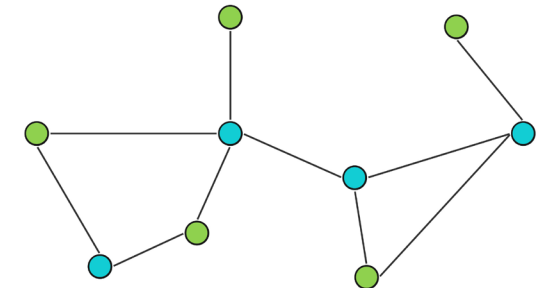
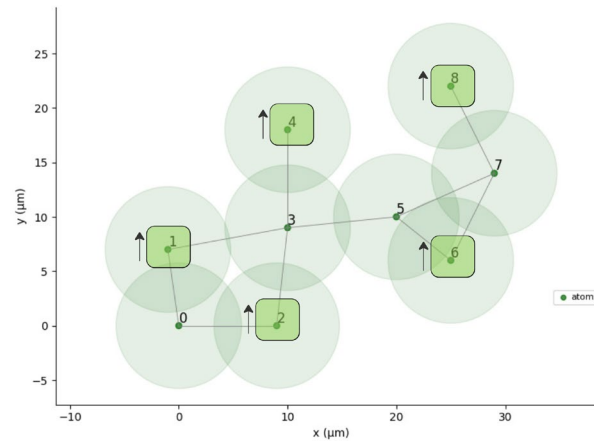
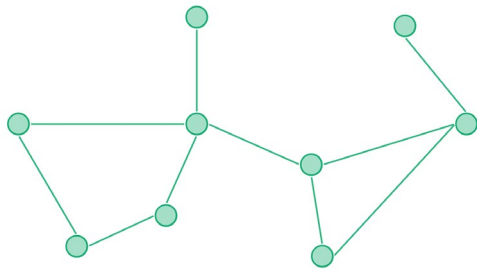


# Solving the MIS on PASQAL QPUs

Maximum Independent Set (MIS) is a well-suited problem for Rydberg atoms

Graph-structured problems are **natively addressable** with neutral atoms !

- Atoms' positions and mutual distances **encode directly** the target graph.
- Rydberg dynamics can be leveraged to naturally encode the **constraints** and solution to the MIS problem for **unit-disk graphs**.





# Perspectives

- Quantum solutions to **real-world industrial problems**,
- Implementations on **real QPUs**, **today**.
- We can **customize or extend existing solutions** to other problems with industrial relevance.



*Towards industry-relevant  
applications on*



Pasqal

*QPU*s

Thank you for your attention